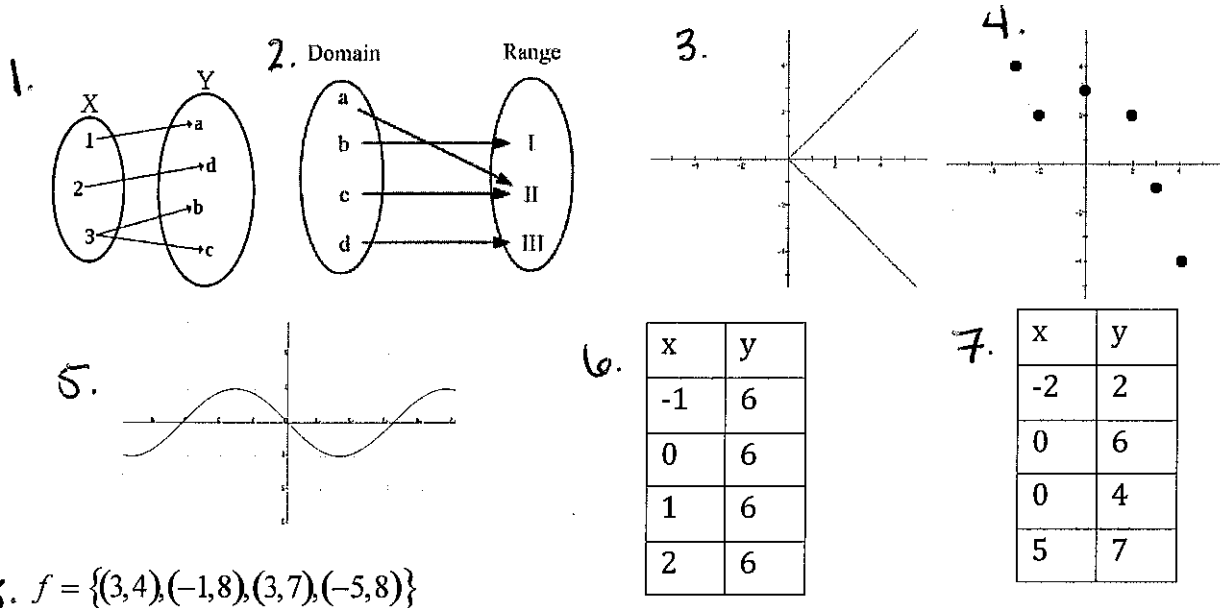


## UNIT 2 REVIEW - FUNCTIONS

### Idea 1 - Are the following functions?



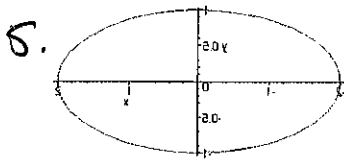
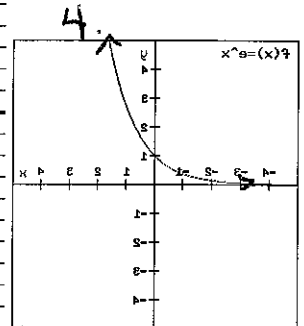
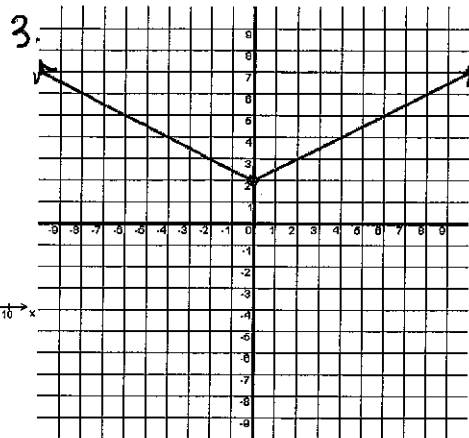
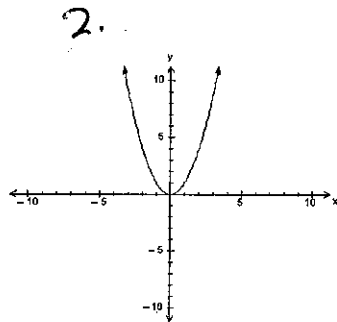
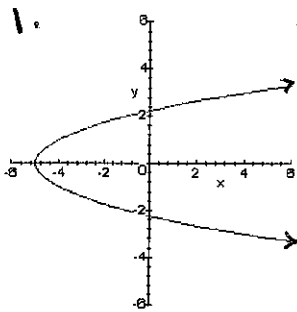
- 9) Which ordered pair  $(x,y)$  makes the following relation a function?  $\{(2,5), (-1,7), (5,3), (-2,6), (x,y)\}$
- A. (2,9)      B. (5,8)      C. (4,7)      D. (-1,10)

### Idea 2 - Combine functions through the 4 operations.

$$f(x) = 9x - 4 \qquad g(x) = 3x^2 - 5x + 7 \qquad h(x) = 8x$$

1. Find  $(f + h)(x)$ . Remember that means  $f(x) + h(x)$ .
2. Find  $(f - g)(x)$ . Remember that means  $f(x) - g(x)$ .
3. Find  $(h \cdot f)(x)$ . Remember that means  $h(x) \cdot f(x)$ .
4. Find  $\left(\frac{g}{f}\right)(x)$ . Remember that means  $\frac{g(x)}{f(x)}$ .
5. Find  $(h - f)(x)$ .
6. Find  $(h \cdot g)(x)$ .
7. Find  $(h + g)(x)$ .
8. The revenue,  $R(x)$ , from selling  $x$  units of a product is represented by the equation  $R(x) = 20x$ , while the total cost,  $C(x)$ , of making  $x$  units of the product is represented by the equation  $C(x) = 8x + 150$ . The total profit,  $P(x)$ , is represented by the equation  $P(x) = R(x) - C(x)$ .  
For the values of  $R(x)$  and  $C(x)$  given above, what is  $P(x)$ ?

**Idea 3 - Give the domain and range for each of the following functions or relations:**



6) Give the interval notation for  $x \leq 5$

7)  $f = \{(3, 4), (-1, 8), (3, 7), (-5, 8)\}$

8. Which value of  $x$  is NOT in the domain of  $y = \frac{6}{x+7}$ ?

**Idea 4 -Evaluating Functions**

$f(x) = 9x - 4$        $g(x) = 3x^2 - 5x + 7$        $h(x) = 8x$

1. Find  $f(3)$

2. Find  $g(-4)$

3. Find  $h(5c)$

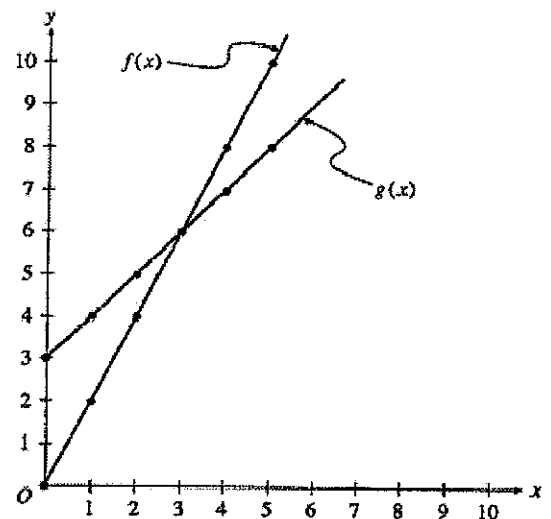
4. Find  $g(d+4)$

5. If  $f(x) = \frac{x^2 - 3x + 6}{x - 1}$ , find  $f(-2)$

6. If  $m(x) = x^{-\frac{1}{4}}$ , then  $m(81)$  is equal to...

7. Which of the following functions will yield the largest value for  $x=20$ ?

- A.  $f(x) = 3^x$       B.  $f(x) = 3 + x$   
C.  $f(x) = 3x$       D.  $f(x) = x^3$



Based on the graph to the right,

8. Find  $g(2)$

9. Find  $f(4)$

### Idea 5 – Composition of Functions

$$f(x) = 9x - 4 \qquad g(x) = 3x^2 - 5x + 7 \qquad h(x) = 8x$$

1. Find  $h \circ f$ . Remember  $h \circ f$  is also written as  $h[f(x)]$ .
2. Find  $f \circ h$ . Remember  $f \circ h$  is also written as  $f[h(x)]$ .
3. Find  $f[h(-4)]$ .
4. Find  $h[g(2)]$ .
5. If  $f(x) = 2x^2 + 4$  and  $g(x) = x - 3$ , which number satisfies  $f(x) = (f \circ g)(x)$ ?

### Idea 6 – Inverse Functions

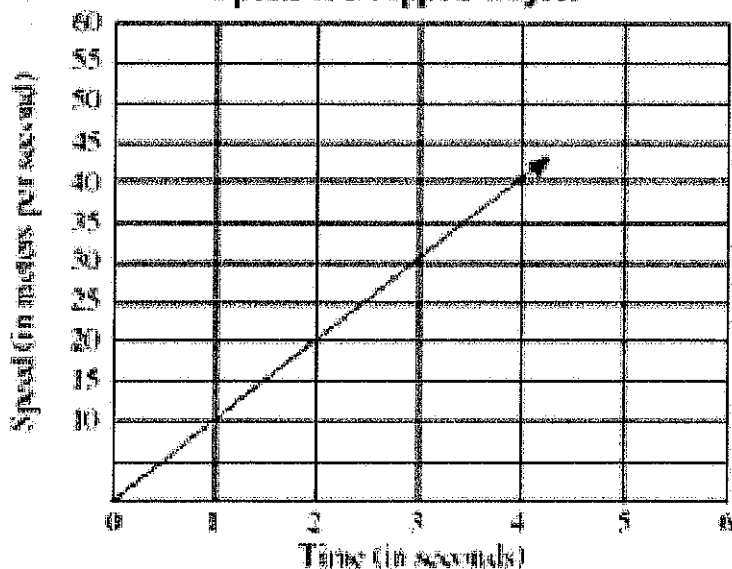
Find the inverse of each function

1.  $l = \{(-4, 2), (6, 7), (5, -1)\}$
2.  $f(x) = -2x + 5$
3.  $g(x) = -\frac{3}{4}x$
4.  $h(x) = x - 7$
5.  $j(x) = \frac{x+9}{4}$
6. Graph the inverse of  $f(x) = \{(0, 4), (-3, 4), (5, 2)\}$

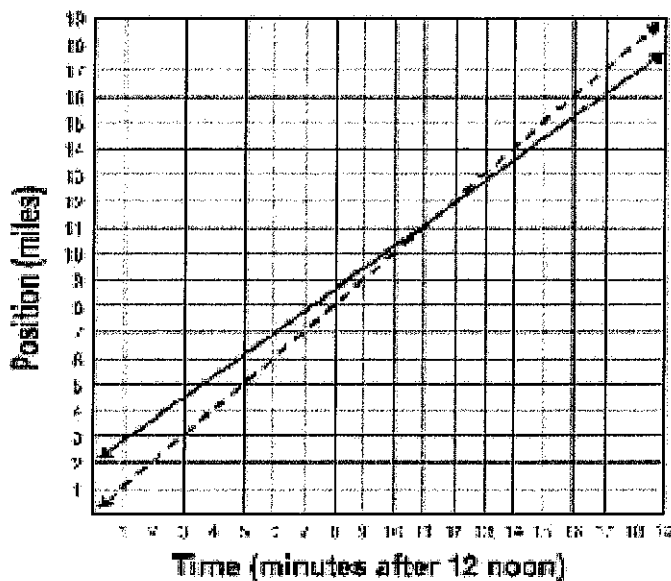
### Idea 7 – Analyzing Graphs

1. Based on the graph, what will be the approximate speed of the dropped object after 6 seconds?
2. At what 2 times are the vehicles exactly 1 mile apart?

Speed of Dropped Object

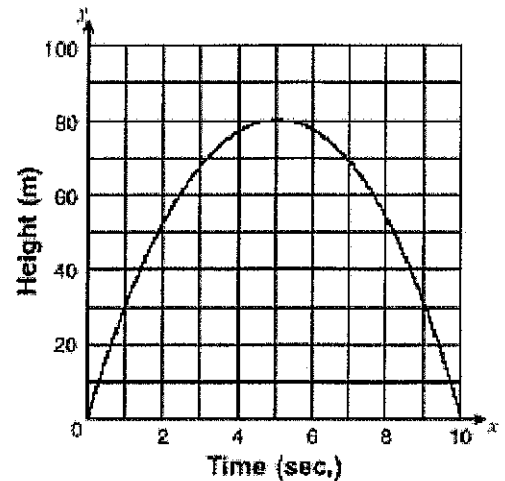


Motion of Car and Truck

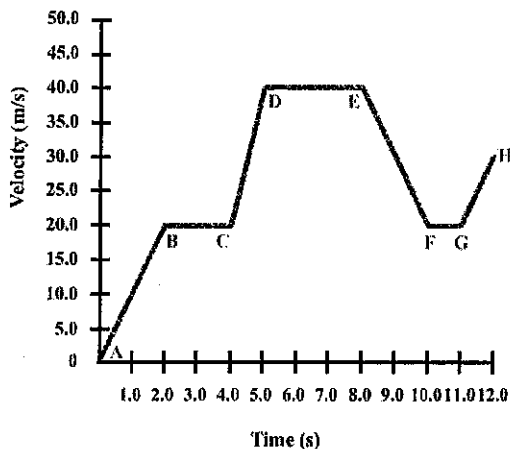


Key	
—	Car
- - -	Truck

3. Based on the graph to the right, estimate the number of seconds for which the projectile was *at least 30 meters high*.



4.



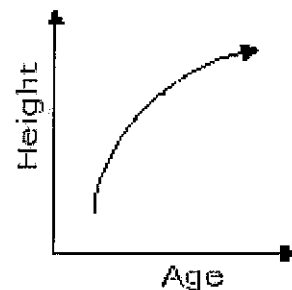
- Name all the segments where the graph shows constant speed.
- When is speed increasing?
- When is speed decreasing?
- When is the object moving the fastest?
- When is the object stopped?

5. Draw a distance vs. time graph to show that I walked away from home at a steady pace for 5 minutes, then turn around and came home at a faster pace.

6. Draw a speed vs. time graph to show a biker who starts out slowly, goes at a constant pace for about 10 minutes, speeds up to a faster constant pace for 20 minutes, then slows to a stop.

7. Describe the rate of change of height vs. age graph shows

- It grows at the same rate every year.
- It grows fastest during its middle years.
- It grows fastest during the first part of its life.
- It grows fastest during its last years.



**Idea 8 – Match up the function families. (There is one capital letter and a double lower case letter for each family name).**

1. Exponential

2. Cubic

3. Linear

4. Sine (Trigonometric)

5. Absolute value

6. Inverse

7. Logarithmic

8. Quadratic

A.  $y = \sin x$

B.  $f(x) = \ln x$

C.  $f(x) = x^3$

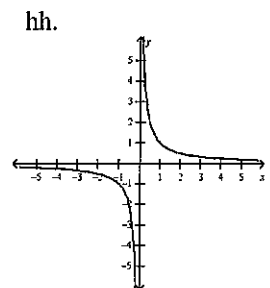
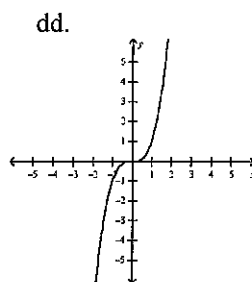
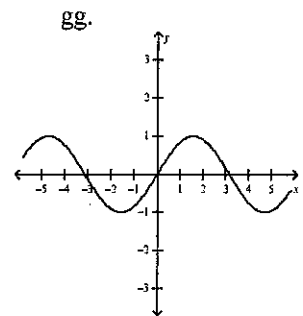
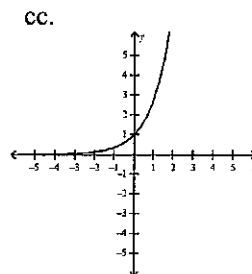
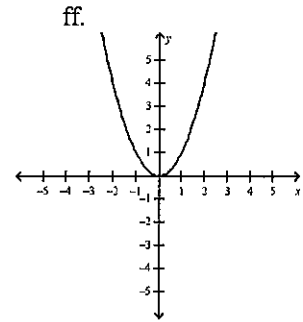
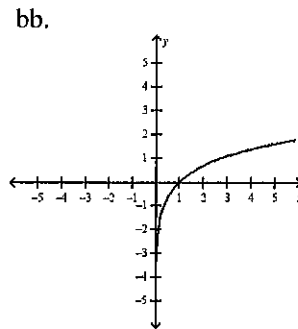
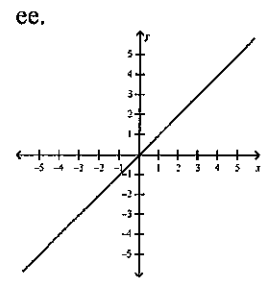
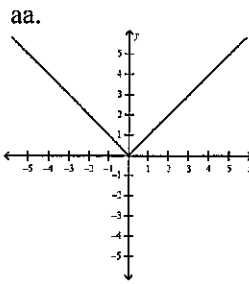
D.  $f(x) = |x|$

E.  $f(x) = \frac{1}{x}$

F.  $f(x) = e^x$

G.  $f(x) = x$

H.  $f(x) = x^2$



## **SOLUTIONS**

### **Answers 1 – Is it a function?**

- 1) no      2) yes      3) no      4) yes      5) yes  
6) yes      7) no      8) no      9) C

### **Answers 2 – Combining Functions Through the 4 Operations**

- 1)  $17x - 4$       2)  $-3x^2 + 14x - 11$       3)  $72x^2 - 32x$       4)  $\frac{3x^2 - 5x + 7}{9x - 4}$   
5)  $-x + 4$       6)  $24x^3 - 40x^2 + 56x$       7)  $3x^2 + 3x + 7$       8)  $P(x) = 12x - 150$

### **Answers 3 – Domain and Range of Functions**

- 1) D:  $[-5, \infty)$       2) D: All real numbers      3) D: All real numbers  
R: All real numbers      R:  $[0, \infty)$       R:  $[2, \infty)$   
4) D: All real numbers      5) D:  $[-2, 2]$       6)  $(-\infty, 5]$   
R:  $(0, \infty)$       R:  $[-1, 1]$   
7) D:  $\{-5, -1, 3\}$       8)  $x = -7$   
R:  $\{4, 7, 8\}$

### **Answers 4 – Evaluating Functions**

- 1) 23      2) 75      3)  $40c$       4)  $3d^2 + 19d + 35$       5)  $-\frac{16}{3} = -5.\bar{3}$   
6)  $\frac{1}{3}$       7) A      8) 5      9) 8

### **Answers 5 – Composition of Functions**

- 1)  $8(9x - 4) = 72x - 32$       2)  $9(8x) - 4 = 72x - 4$       3)  $f[h(-4)] = f(-32) = -292$   
4)  $h[g(2)] = h(9) = 72$       5)  $x = \frac{3}{2}$

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**Answers 6 – Inverse functions**

1)  $f^{-1} = \{(2, -4), (7, 6), (-1, 5)\}$

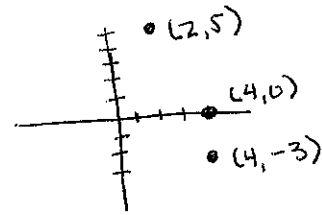
2)  $f^{-1}(x) = \frac{x-5}{-2} = -\frac{1}{2}x + \frac{5}{2}$

3)  $g^{-1}(x) = -\frac{4}{3}x$

4)  $h^{-1}(x) = x + 7$

5)  $j^{-1}(x) = 4x - 9$

6)

**Answers 7 – Analyzing Graphs**

1) 60 meters per second

2) 12:06 and 12:18

3) 8 seconds

4) A. BC, DE, FG

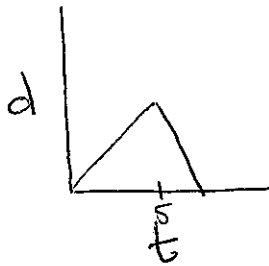
B. AB, CD, GH

C. EF

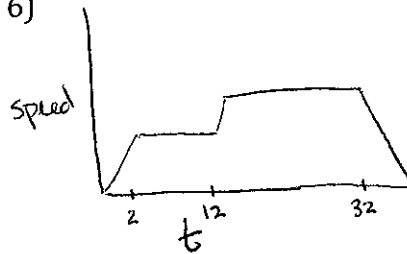
D. DE (speed of 40 m/s)

E. Never

5)



6)



7) C

**Answers 8 – Function Families**

1) F, cc

2) C, dd

3) G, ee

4) A, gg

5) D, aa

6) E, hh

7) B, bb

8) H, ff